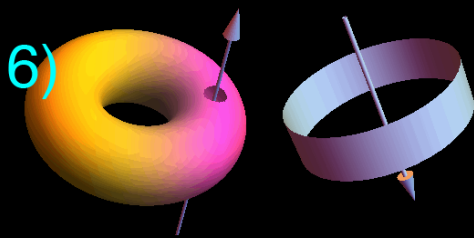




*Physics of bulk-edge correspondence & its universality (BEC2016)*

*From solid state physics to cold atoms Workshop 2016, Sep 27-30*



Kyoto, Sep.27 (2016)

**Welcome everybody !**

**YITP international workshop**  
**“Physics of bulk-edge correspondence**  
**& its universality :**  
**From solid state physics to cold atoms”**  
**(BEC2016)**

**Devison of Physics, University of Tsukuba**  
**Yasuhiro Hatsugai**

京都大学 基礎物理学研究所

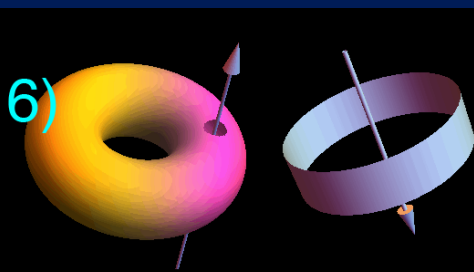
Yukawa Institute for Theoretical Physics Kyoto University

科研費  
KAKENHI



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**This workshop is supported by**  
**Yukawa Institute for Theoretical Physics (YITP)**  
**& KAKEN-HI (JSPS)**

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Yukawa Institute for Theoretical Physics Kyoto University

科研費  
KAKENHI

**BEC**

**B**ulk-**E**dge **C**orrespondence

*named by K.-I. Imura*

---

**B**ose **E**instein **C**ondensation

*well established*

---

**B**ulk **E**dge **C**orrespondence

*not yet*

*Implying we have a dream*

# *BEC 2015 Tokyo*

*Last year*

*Solid state, photonics & cold atoms*

---

# *BEC 2016 Kyoto*

*Solid state, photonics & cold atoms*

*+ Newton's      + Maxwell's*

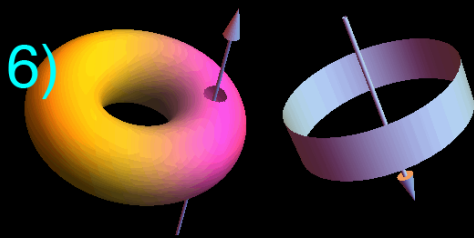
*+ Math*

*Exchange idea between different area !*



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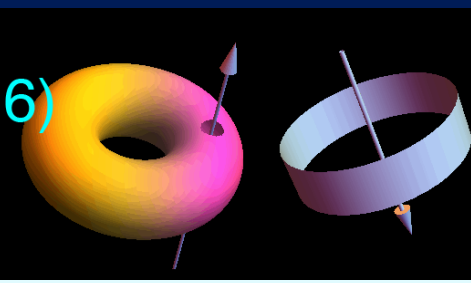
**Welcome everybody !**

**Thank you for joining us**

**Just a few words before the tight schedule**

**“ Bulk-edge correspondence :  
From math to physics & beyond ”**

**Devison of Physics, University of Tsukuba  
Yasuhiro Hatsugai**



**Welcome everybody !**

Thank you for joining us

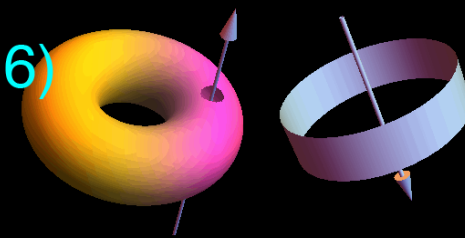
Solid states

Topological states

Photonics & Newton's !

Cold atoms





# Welcome everybody !

Thank you for joining us

Solid states

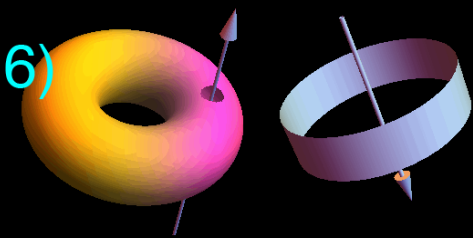
Topological states

Photonics & Newton's !

Cold atoms

As a bulk

- ★ Hidden
- ★ Can not be seen
- ★ Gapped
- ★ Unconventional



# Welcome everybody !

## Thank you for joining us

### With edges

- ★ Observables
- ★ In gap states
- ★ Low energy modes

### Solid states

### As a bulk

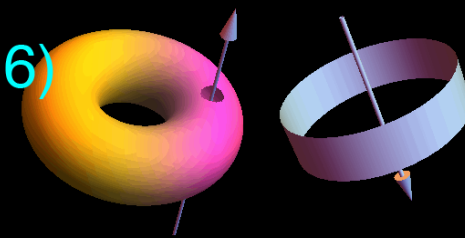
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### Topological states

### Photonics & Newton's !

### Cold atoms





# Welcome everybody !

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### With edges

- ★ Observables
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- ★ Low energy modes

### Solid states

### As a bulk

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- ★ Can not be seen
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## bulk-edge correspondence

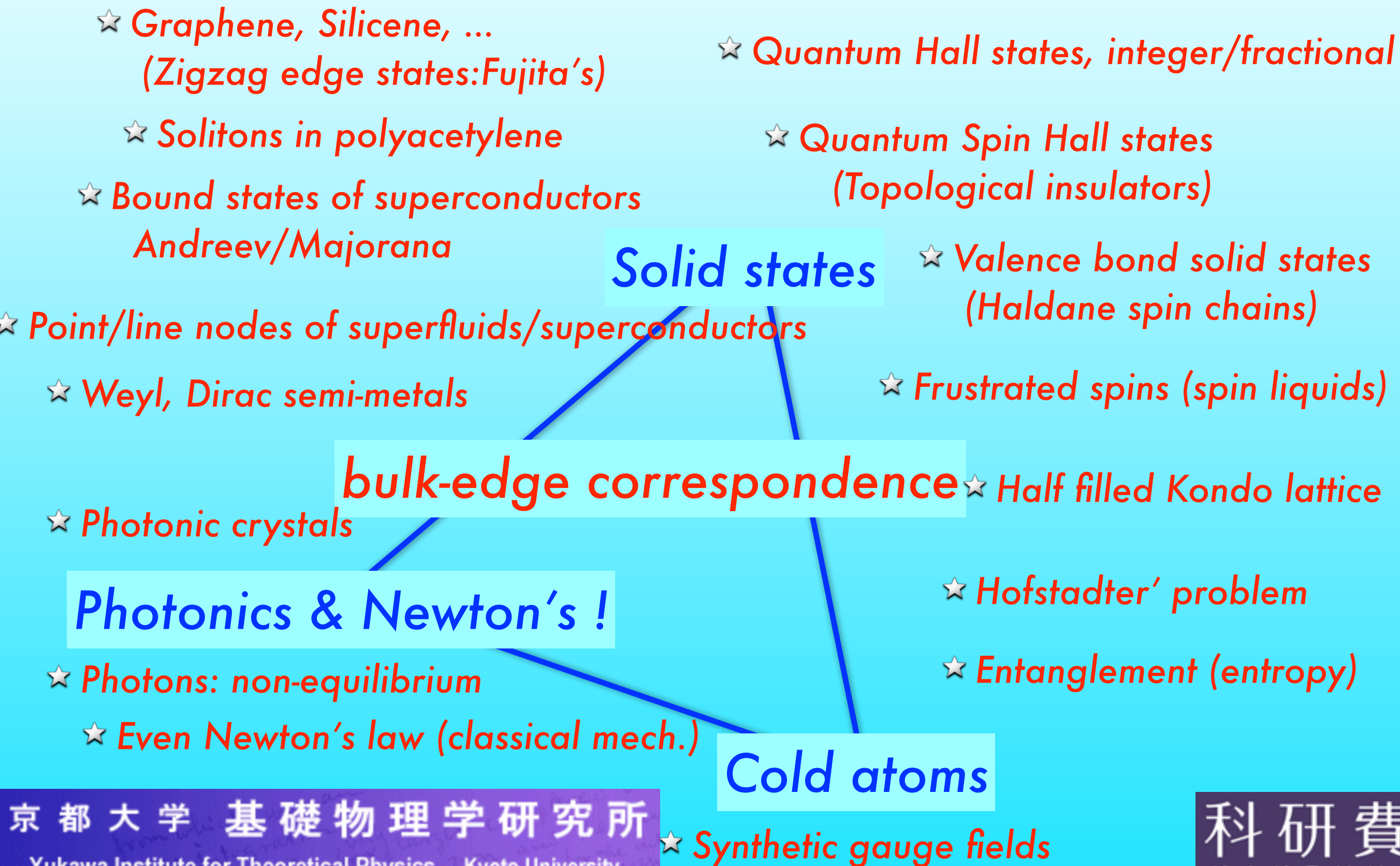
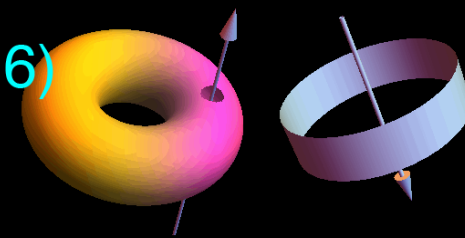
### Photonics & Newton's !

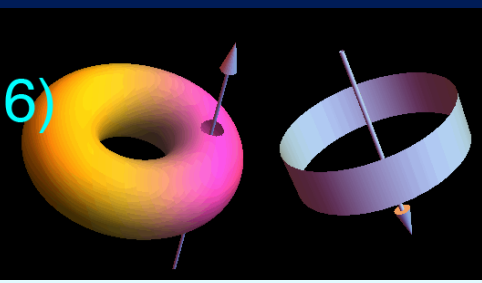
### Cold atoms



# Physics of bulk-edge correspondence & its universality (BEC2016)

From solid state physics to cold atoms Workshop 2016, Sep 27-30





# Diversity / Everywhere ? !

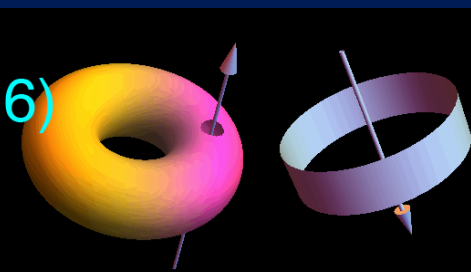
Lots of fun to play with

Solid states

bulk-edge correspondence

Photonics & Newton's !

Cold atoms



Learn something from examples !

# From diversity to **UNIVERSALITY**

Solid states

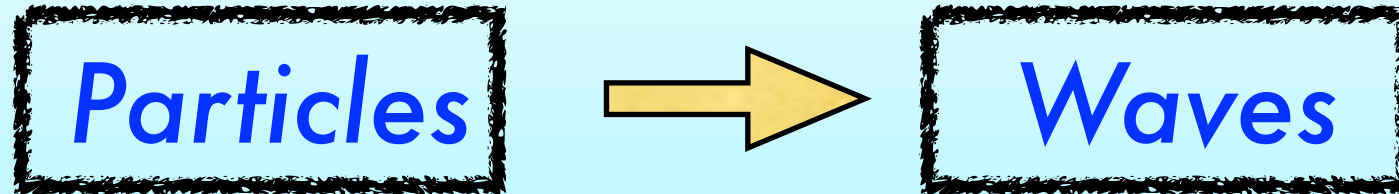
bulk-edge correspondence

Photonics & Newton's !

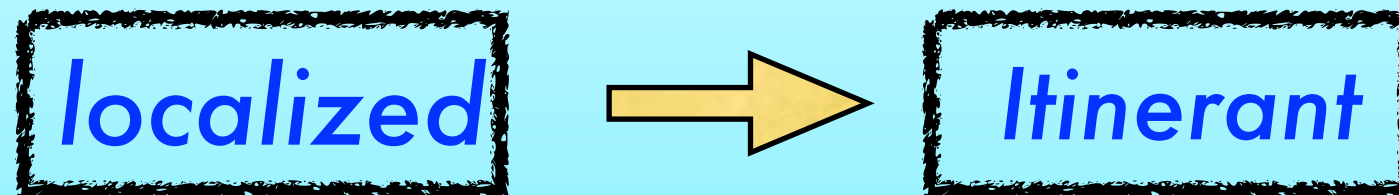
Cold atoms

# 20-th century

Quantization:



*photons, magnons, excitons, phonons, polaritons, spin wave...*

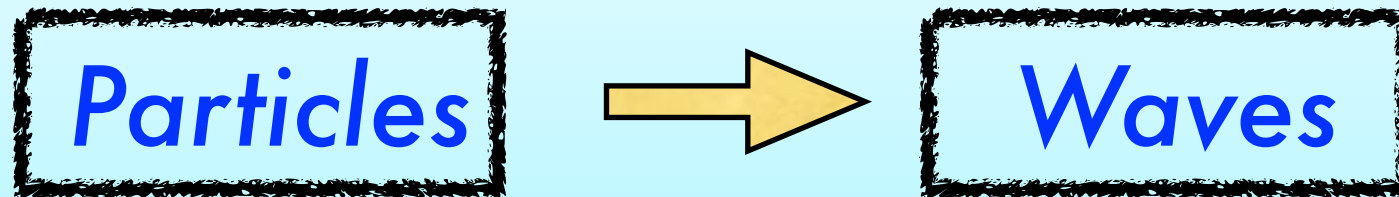


*gapless excitations*

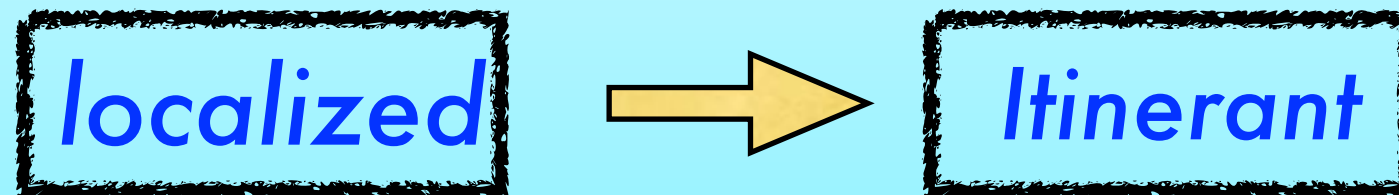


# Before 80'

## Quantization:



photons, magnons, excitons, phonons, polaritons, spin wave...



gapless excitations

☑ Metal is *IMPORTANT* and insulators are not !

☑ Thermodynamic limit is *IMPORTANT* Anderson  
Nambu

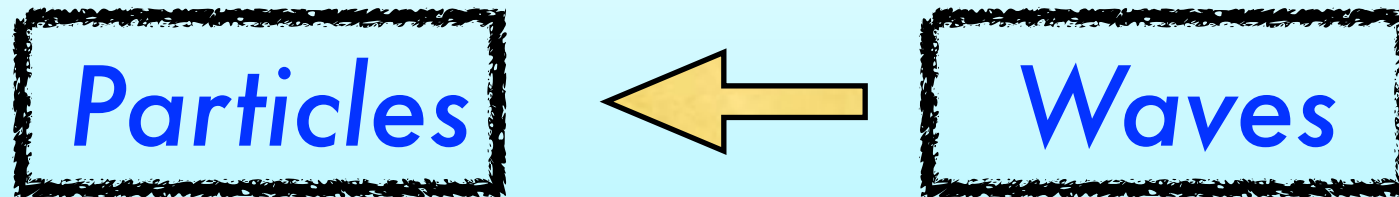
More is different / Symmetry breaking

Huge success ! Universal idea over whole physics

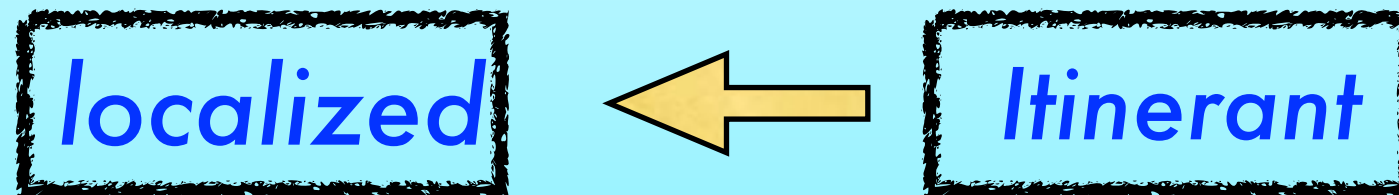
From magnetism to superconductivity: Landau-Ginzburg-Wilson

# After '80

Back to "classical world"



Q(S)HE, superconductivity, spin gap, Haldane gap,



*gapped*



*No Response*

Anderson

Nambu

More is different / symmetry breaking

Huge success ! Universal idea over whole physics

But, but,....

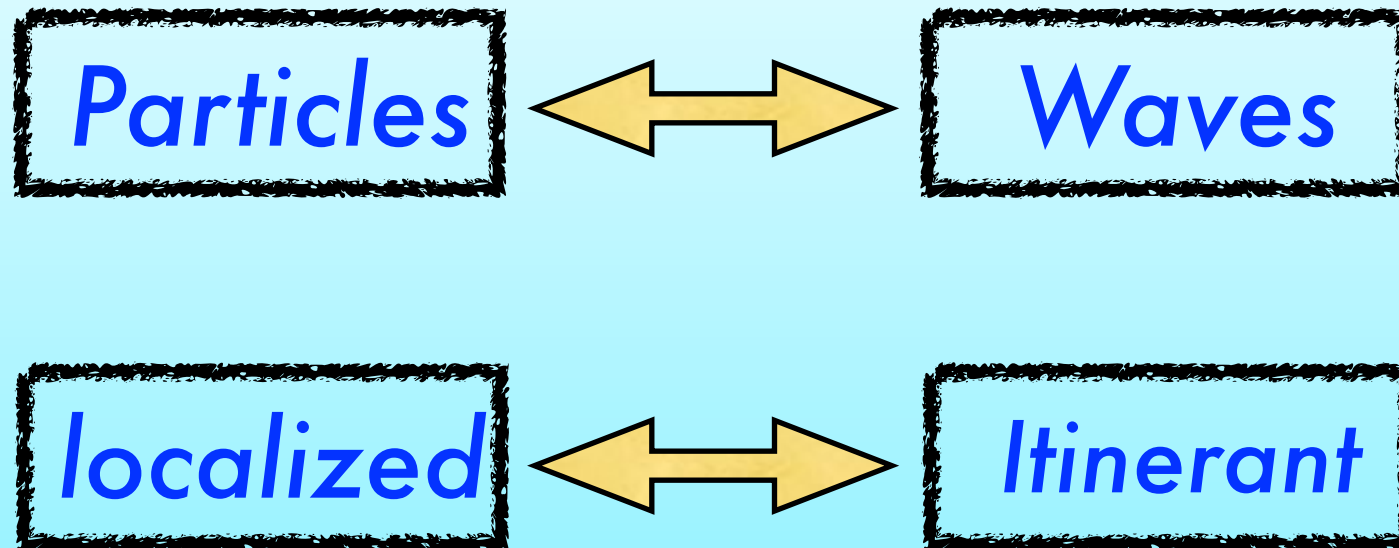
**We do have gapped systems everywhere!**

**NEED something for classification**

- Topological order
- Berry connections
- Edge states

*Now we are in the new millennium*

 *Think different ! : topological phases*



*related with each other*

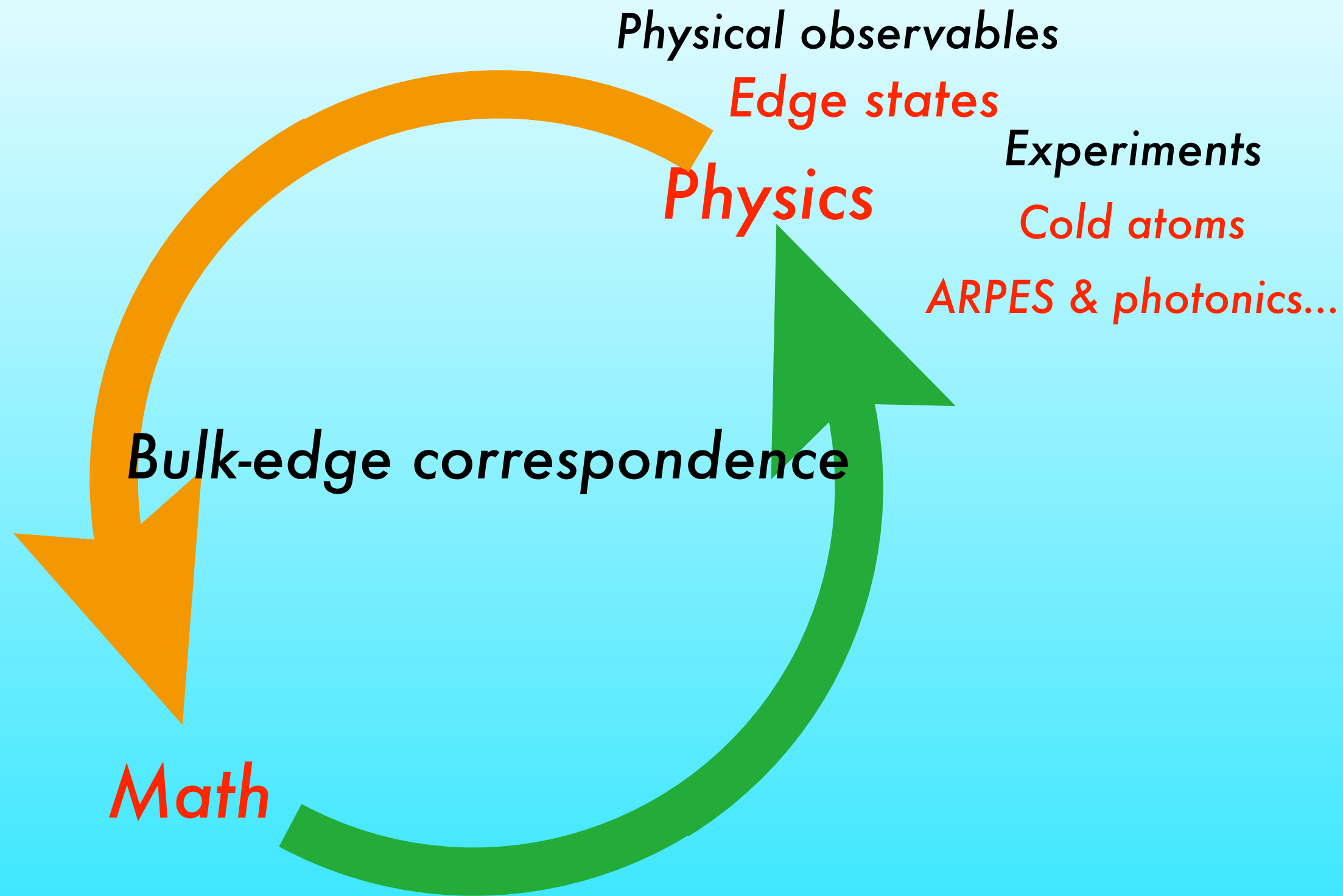
*Lots of varieties for gapped systems (noticed just recently)*

- Insulators (superconductors) can be of fun !*
- Boundaries are not negligible*

*Bulk-edge correspondence*

# Math & physics :BEC2016

Exchange idea between different area !



New idea for better understanding of the matter

# Math & physics :BEC2016

Exchange idea between different area !

Physical observables

Edge states

Experiments

Cold atoms

ARPES & photonics...

Physics

Bulk-edge correspondence

Math

$U(1)$ ,  $sp(1)$ , chiral ...

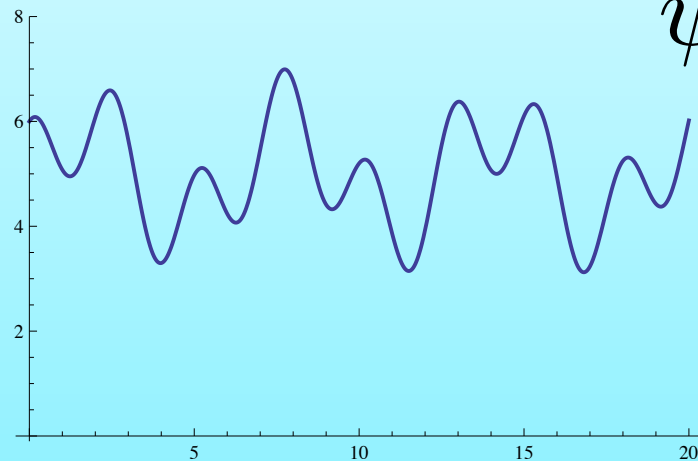
+ symmetry protection

New idea/phenomena : "adiabatic principle"



# Edges states vs bulk states ( $V \rightarrow \infty$ )

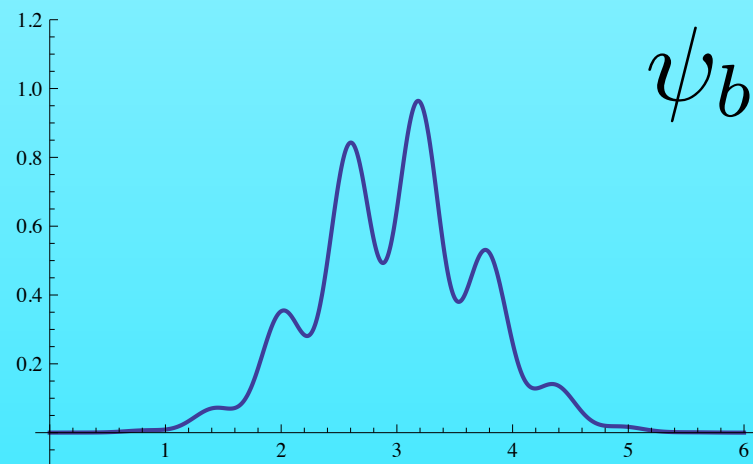
**Extended states / bulk states**      **unnormalizable**



$$\psi_e(r) \sim \frac{1}{\sqrt{V}} e^{ikr} \longrightarrow 0 \quad (V \rightarrow \infty)$$

$V$ : Volume of the whole system

**Bound states / Edge states**      **normalizable**



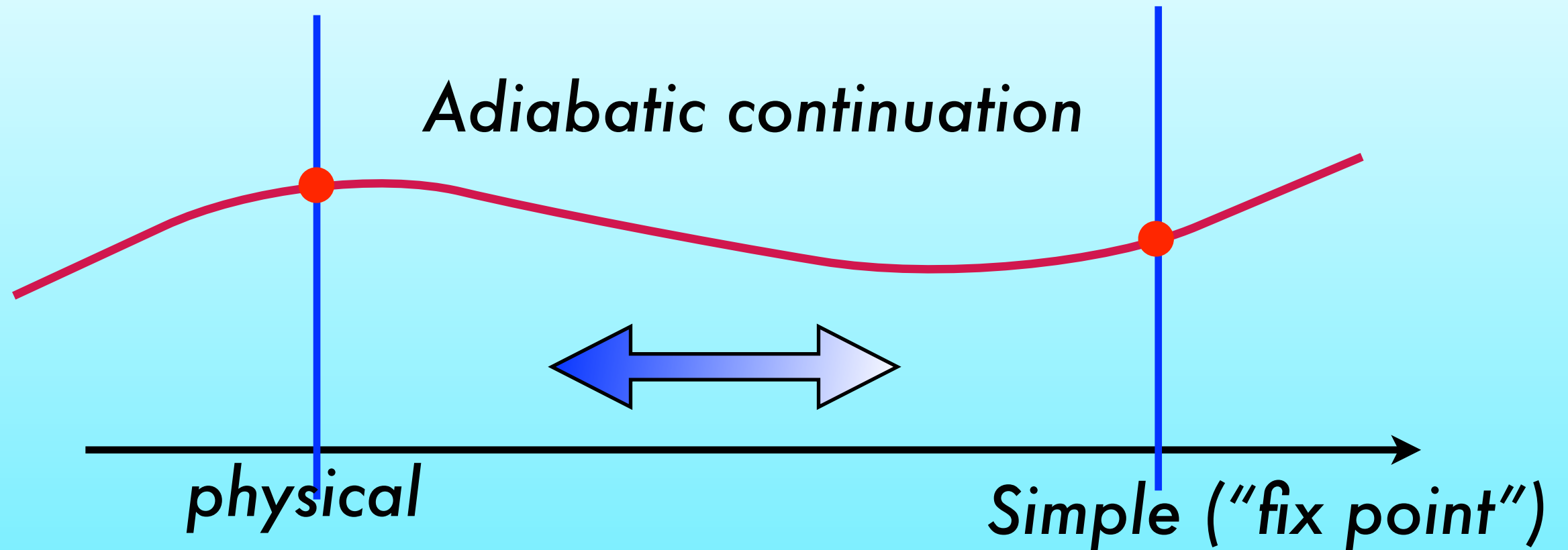
$$\psi_b(r) \sim \frac{1}{\sqrt{a_0^3}} e^{-r/a_0}$$

$a_0$  : size of the bound state

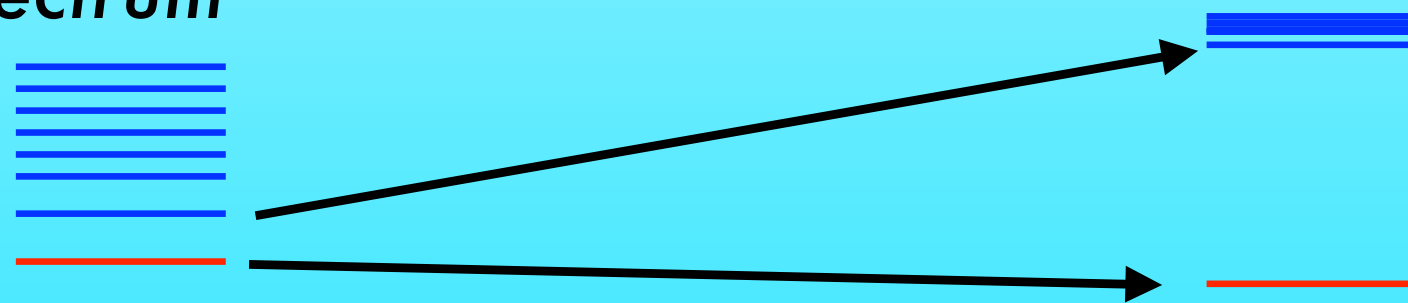
Clear difference **only** in the **infinite** system with boundaries !

# Adiabatic principle

*For bulk*



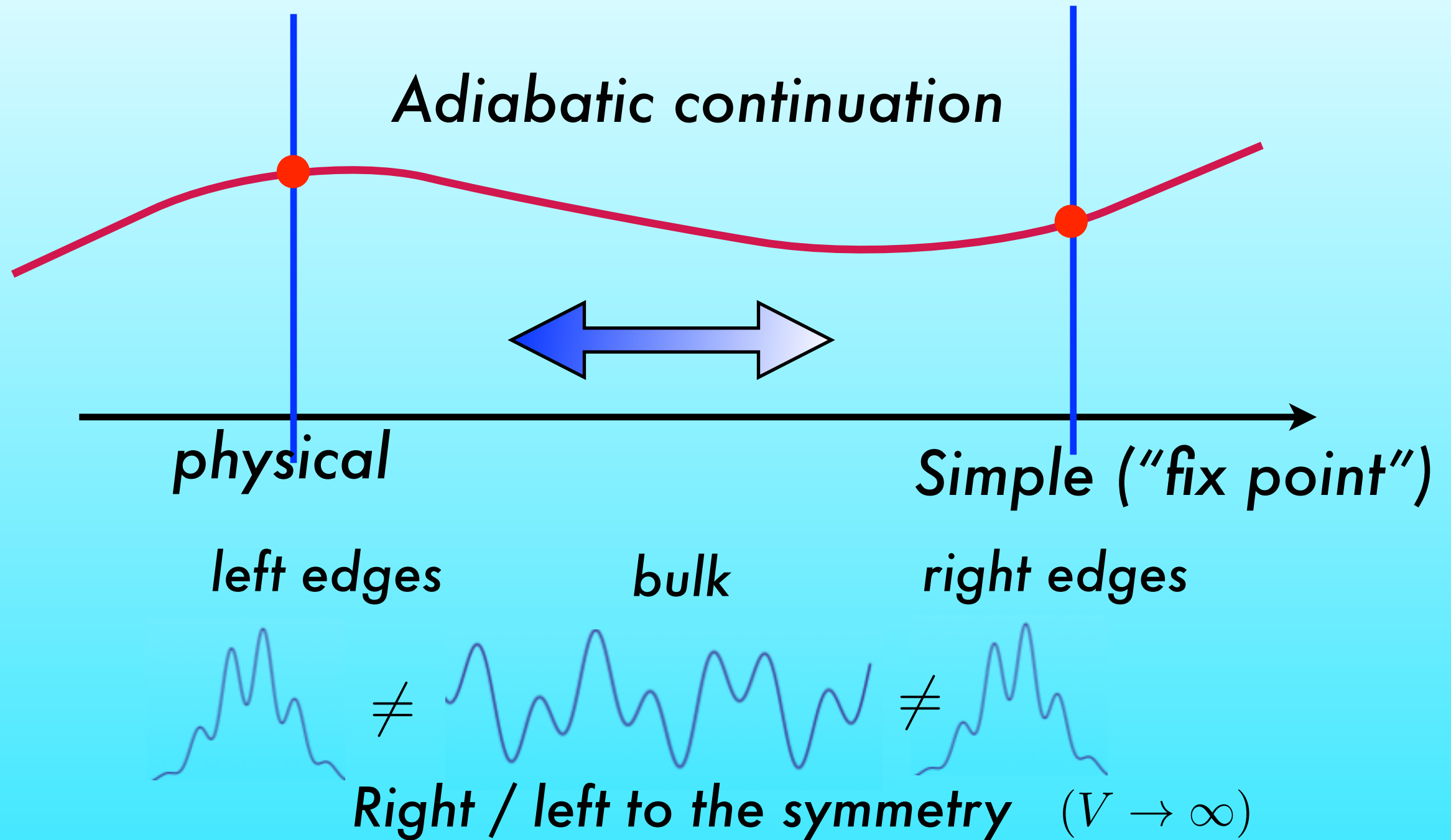
Manybody spectrum



Quantized quantity (Chern #,..) : Adiabatic invariant remains the same, unless the gap closes.

# Adiabatic principle

For edges

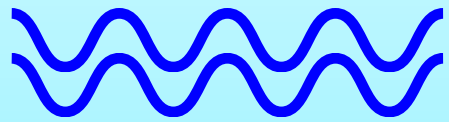


Edge states (in the gap) can not disappear suddenly unless the gap closes

Edge states are adiabatic invariants if the bulk is gapped !

*Edge states: need some reasons to be there !  
Not accidental !*

## *Bulk-edge correspondence*



*Bulk state*  
*"vacuum"*

*Universality*

*Control*  
*with*  
*each other*

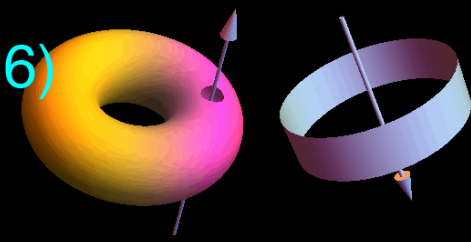


*Edge state*  
*"particles"*

*Edge state is a topological order parameter*

*Understand the bulk from edges*

*Edge determines the bulk*



# Summary

Learn physics/math from examples

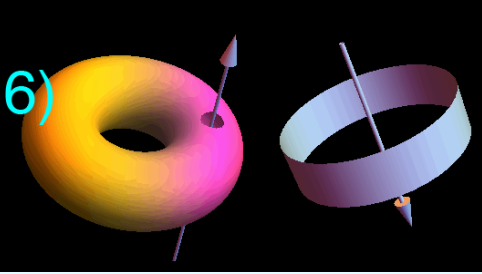
Solid states

bulk-edge correspondence

Photonics & Newton's !

Cold atoms





**Enjoy this workshop!**

**Learn physics/math from examples**  
a common key word

**Math**

**Physics**

**Bulk-edge correspondence**