

## 7 終わりに

以上時間の関係上省略した話題も多いが、磁場中の電子系の問題は、物性物理と数理的構造とのいくつかの意外な関係を見せてくれたことは伝えられたものと期待したい。歴史的にはこの問題に関して、もう調べ尽くされたと思えた時期も何度かあったがそのたびに新しい発見があり、驚きをとまなう興味深いブレークスルーが何度もくりかえされてきたのである。私には、未だ明らかになっていない興味深い構造がまだそこにあるかのように思えるが、みなさんにとっては如何であろうか。

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